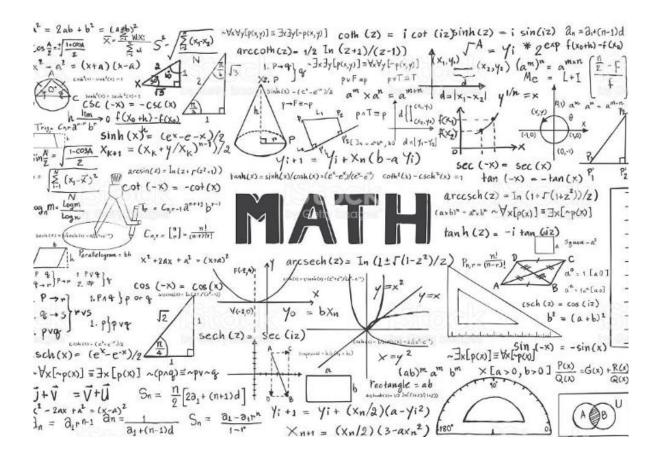




Essential Topics A Level Mathematics



Name

You must complete this booklet and bring it with you to your first class in September

Skills you should have

Below is the list of the skills you should be confident with before starting the A-level maths course:

Basic algebra (non-calculator)

- simplifying algebraic expressions by collecting like terms
- general laws of indices
- expanding and factorising expressions (one term outside)
- laws of indices for all rational exponents (positive, negative, fractions)

Quadratic functions (non-calculator)

- plotting graphs of quadratic functions
- expanding and factorising quadratics (two brackets)
- solving quadratic equations by factorising
- solving quadratic equations using the formula

Equations and inequalities (non-calculator)

- solving simultaneous linear equations by elimination
- solving simultaneous linear equations by substitution
- solving linear inequalities

Sine rule and cosine rule (calculator allowed)

- using the sine rule to find missing sides and angles
- using the cosine rule to find missing sides and angles
- using sine rule, cosine rule, trig ratios and Pythagoras in problems

These are all GCSE topics so there is nothing here which you have not already covered.

In this booklet we have four sections of questions to help you keep up to date. Please complete and bring with you to hand in on the June induction days.

Section A

These are all questions that you should definitely be able to answer, even if you have to refresh your memory with your books.

Section **B**

A second set of questions which are slightly harder, but you should be able to have a good go.

Section C

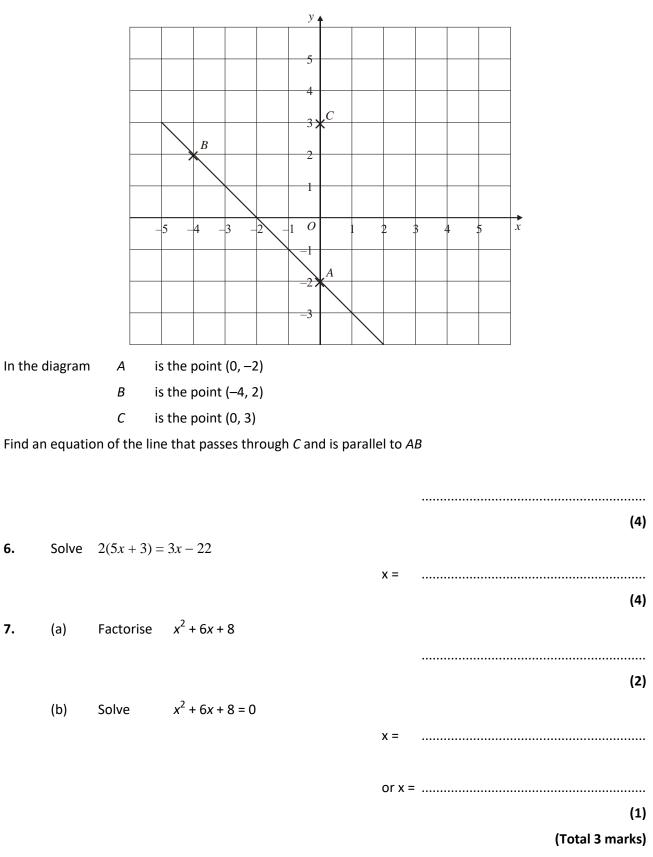
Harder Grade 8 and 9 questions. Just see what you can do!

Section D

Some calculator work using trigonometry, the sine and cosine rule.

Section A (definitely)

1.	(a)	Work out the value of $\frac{2}{3} \times \frac{3}{4}$		
	Give y	our answer as a fraction in its simplest form		
				(2)
	(b)	Work out the value of $1\frac{2}{3} + 2\frac{3}{4}$		
	Give y	our answer as a fraction in its simplest form		
				(3)
				(Total 5 marks)
2.	(a)	Simplify		
		(i) $\rho^2 \times \rho^7$		
		(ii) $x^8 \div x^3$		
		(iii) $\frac{y^4 \times y^3}{y^5}$		
		y^5		
				(3)
	(b)	Expand $t(3t^2+4)$		
				(2)
_		24		(Total 5 marks)
3.	Simpl	fy fully $(3xy^2)^4$		
4.	Solve	the simultaneous equations		(2)
	2x + 3			
		y = 22		
		, ,	<i>x</i> =	
			y =	
				(4)



Section B (should be able to...)

1.

(a) Complete the table for $y = x^2 - 3x + 1$

	4	3	2	1	0	-1	-2	X
	5	1		-1	1		11	у
(2)			+ 1	$y = x^2 - 3x - 3x$	graph of y	s draw the	a set of axe	(b) On :
(2)		lue of y	inimum va	e for the m	an estimate	oh to find a	e your gra	(c) Us
			y = .					
(1)								
(Total 5 marks)								
					4 <i>x</i> – 5.	uation $y = 4$	line has eq	A straight
					y = 1.	of <i>x</i> when <u>y</u>	the value	(a) Finc
		• • • • • • • • • • • • • • • • • • • •	x = .					
(2) asses through		lel to <i>y</i> = 4	nat is paral	aight line tl	of the stra			
	x – 5 and p			aight line tl o find <i>x</i> in t			point (0, 3)	the
asses through	x – 5 and p						point (0, 3)	the
asses through 	x – 5 and p		erms of y. x =		v = 4x − 5 to	equation y	point (0, 3) rrange the	the (c) Rea
asses through (2)	x – 5 and p	3	erms of y. x =	o find <i>x</i> in t	y = 4x - 5 to	equation y	point (0, 3) rrange the all the pos	the (c) Rea (a) List
asses through (2) (2) (Total 6 marks)	x – 5 and p	3	erms of y. x =	o find <i>x</i> in t	y = 4x - 5 to	equation y	point (0, 3) rrange the all the pos	the (c) Rea (a) List

4.	(a) Solve $\frac{40-x}{3} = 4 + x$		
	(b) Simplify fully $\frac{4x^2-6x}{4x^2-9}$	x =	(3)
			(3) (Total 6 marks)
5.	Make <i>u</i> the subject of the formula $D = ut + kt^2$		
		u =	
6.	Work out $\frac{(5+\sqrt{3})(5-\sqrt{3})}{\sqrt{22}}$		(2)
	Give your answer in its simplest form.		
			(3)
7.	(a) Write $x^2 + 12x - 5$ in the form $(x + a)^2 + b$		
	(b) Hence or otherwise solve the equation $x^2 + 12x - 12x $	-5 = 0	(2)
			(2)
			(Total 4 marks)

Section C (might be able to...)

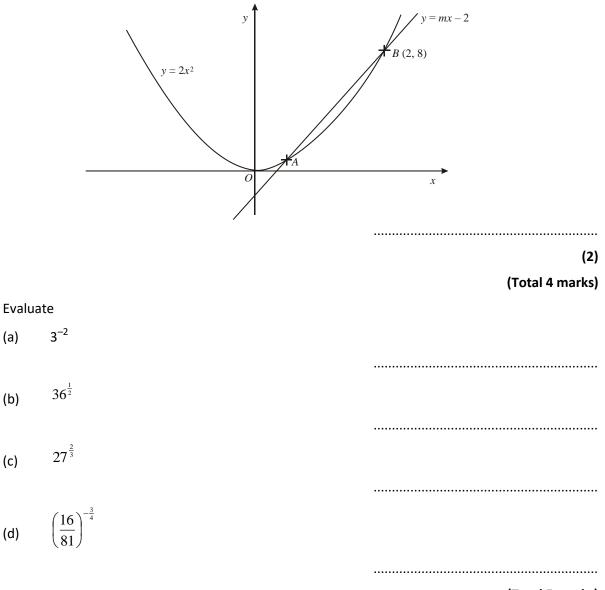
y =	
	(7)

5. (a) Find the equation of the straight line which passes through the point (0, 3) and is perpendicular to the straight line with equation y = 2x

.....

(2)

The graphs of $y = 2x^2$ and y = mx - 2 intersect at the points A and B. The point B has (b) coordinates (2, 8). Find the coordinates of the point A.



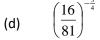
(Total 5 marks)

(b)

(a)

6.

(c)



7. Peter cuts a square out of a rectangular piece of metal

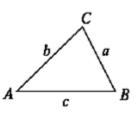
		2x + 3	Dia survey NOT
		x+2 $x+2$ $x+2$	Diagram NOT accurately drawn x + 4
The w The le	idth of t ngth of t	the rectangle is $2x + 3$ the rectangle is $x + 4$. The side of the square is $x + 2$. The side in centimetres.	
The sh	naded sh	ape in the diagram shows the metal remaining.	
The ar	ea of th	e shaded shape is 20 cm ² .	
(a)	Show	that $x^2 + 7x - 12 = 0$	
			(4)
(b)	(i)	Solve the equation $x^2 + 7x - 12 = 0$	
		Give your answers correct to 4 significant figures	s
			(3)
	(ii)	Hence, find the perimeter of the square	
		Give your answer correct to 3 significant figures.	
			cm
			(1)
			(Total 8 marks)

In any triangle ABC

Area of triangle = $\frac{1}{2}ab \sin C$

Since rule $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule $a^2 = b^2 + c^2 - 2bc \cos A$

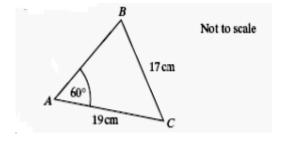


1. *ABC* is a triangle

AC = 19 cm

BC = 17 cm

Angle $BAC = 60^{\circ}$



Calculate the size of angle ABC

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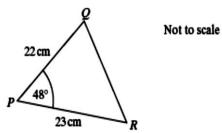
(3)

2. *PQR* is a triangle

PR = 23 cm

PQ = 22 cm

Angle QPR = 48°

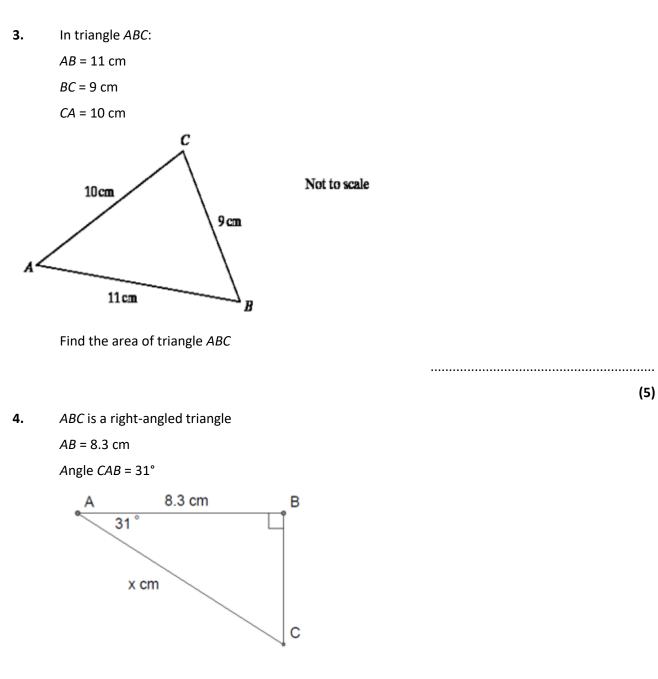


Calculate the length of QR

Give your answer to an appropriate degree of accuracy

.....

(4)



Find the length of AC (marked x in the diagram). Give your answer to a suitable degree of accuracy

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